Pharmacological treatment of chronic conditions often is a form of a recurrent trial and error. Typically, a physician administers a standard initial dose and observes the patient for a specific response and/or the occurrence of a side effect. Subsequently, the drug dose is adjusted in order to achieve a better response or to eliminate the dangerous side effect. This process continues until a desired response is obtained. The goal of this article is to provide and customize an efficient computational framework, based on reinforcement learning, to formalize this trial-and-error process.

Anemia due to end-stage renal disease (ESRD) is a common chronic condition in patients receiving hemodialysis [1]. It occurs due to an insufficient availability of a hormone called erythropoietin (EPO), which stimulates the production of red blood cells (erythropoiesis). The preferred treatment of renal anemia consists of external administration of recombinant human erythropoietin (rHuEPO). The Dialysis Outcomes Quality Initiative of the National Kidney Foundation recommends that the hemoglobin (Hgb) level in patients receiving rHuEPO be maintained between 11 and 12 g/dL. To follow these guidelines, dialysis units develop and maintain their own anemia management protocol (AMP).

Untreated, anemia can lead to a number of conditions including heart disease [2], [3], decreased quality of life [4], and increased mortality [5]. The sequencing and cloning of the human EPO gene and the subsequent availability of rHuEPO greatly improved morbidity and mortality for hemodialysis patients [6]–[8]. Prior to the clinical use of rHuEPO, chronic renal failure patients were the largest consumers of red blood cells. Ninety percent of dialysis patients require supplemental rHuEPO for the treatment of their anemia. In the United States, the cost of rHuEPO for treating these 320,000 dialysis patients exceeds US$1 billion annually [9].

Reinforcement learning is a computational approach that mimics a goal-oriented skill acquisition performed by humans and animals [10]. It represents the notion of goal-oriented learning by considering an agent; i.e., an intelligent decision system that interacts with an environment to achieve a specific goal through a trial-and-error process. Adopting this point of view for the drug administration problem, the agent represents the physician and the patient represents the environment. The process of administering the dose and observing the response corresponds to the trial-and-error aspect of learning. Applications of goal-oriented learning methods to drug administration have surfaced in the literature only very recently [11], [12]. We have recently proposed the use of two mainstream reinforcement learning methods to facilitate the individualization of anemia management. In [13] we have demonstrated that an on-policy reinforcement learning approach is capable of discovering appropriate dosing strategies for individuals with different responses to rHuEPO. On the other hand, in [14], we have shown that an off-policy reinforcement learning approach performs rHuEPO administration almost as well as the AMP that is currently used at our dialysis unit. These preliminary results made it possible for us to identify which aspects of the reinforcement learning algorithms can be further customized to better fit this specific application.

In this work, which is an extension of [15], we present an approach that incorporates prior knowledge about the dose-response characteristic of the patient into the learning. It is known that the dose-response curve of Hgb versus EPO has a monotonic shape [1]. For example, if the Hgb response is insufficient after a starting rHuEPO dose, the physician knows that the next dose should be higher. Consequently, an understanding of the processes that controls red blood cell production tells us in what direction a dose adjustment should take but not the size of the adjustment. The Q-learning algorithm, such as the one used in [14], is not able to utilize this type of prior knowledge. This may lead to suboptimal treatment outcomes.

Guiding reinforcement learning with external knowledge has been a major issue for over a decade. Many researchers have adopted the term advice to identify this type of knowledge provided/imposed by an external source. Two natural problems that arise when dealing with advice are how to represent it and where to incorporate it in the learning system. Maclin and Shavlik [16] proposed a reinforcement learning system that requests advice from an external observer and assimilates the provided information in its internal structure. On the other hand, a learning scheme augmented with an explicit supervisor is presented in [17]. This study addresses the issue of combining the supervisor knowledge with the reinforcement signal in an optimal
Reinforcement learning is a computational framework that mimics trial-and-error learning performed in humans and animals.

way. These two works present and delineate very sound scenarios of utilizing advice, which is however provided on-the-fly, not a priori. In our problem, we consider another form of advice, which originates from clinical practice and gives rise to an efficient abstraction, simplifying the search for an optimal dosing policy. We propose a simple modification to \( Q \)-learning to allow for the use of prior information about the character of the Hgb versus EPO curve. We expect that this modification will make the rHuEPO dosing more efficient.

Understanding the Data

The proposed simulation scenario for the dosing of EPO is shown in Figure 1. The dynamics governing the behavior of Hgb are represented by the block denoted “Patient” and are influenced by two factors: the administered rHuEPO dose and available iron needed to make red blood cells measured by the transferrin saturation (TSat). The key element of the proposed method is represented by the block labeled “\( Q \)-learning Agent.” This agent’s task is to acquire the best dosing policy; i.e., the dose of rHuEPO for each possible Hgb level that will achieve the goal of the therapy. This policy is evolved during sequential observations of the Hgb changes in “Patient” as a result of changing rHuEPO dose. After an rHuEPO dose is administered to “Patient,” a corresponding change of Hgb level occurs. The direction and the amount of this change are used by “\( Q \)-learning Agent” to improve the current policy. In this work, the policy is represented by a look-up table that relates the Hgb levels to the corresponding rHuEPO amounts; thus, it is a coarse policy. On the other hand, the Hgb levels observed in “Patient” are continuous. To allow for gradual dose changes, the “Dose Administration” block performs an interpolation to find an intermediate dose, should the actual Hgb level lie between the levels represented in the coarse policy.

The goal of the treatment is to drive the Hgb level in a patient to within the target range of 11 to 12 g/dL and maintain it within this range by adjusting the amount of rHuEPO administered. For the purposes of this work we chose the desired Hgb as the midpoint of this range, 11.5 g/dL. As noted above, the Hgb response is also influenced by the TSat, measured in percent, and represented in this work as a normal random variable with mean \( m_{TSat} \) and standard deviation \( \sigma_{TSat} \).

Translating this formulation into a state-space notation, frequently used in control theory, Hgb and TSat become state variables and rHuEPO becomes the control variable. In the proposed simulation scheme, “Patient” is represented by a stochastic iteration,

\[
Hgb[k+1] = f(Hgb[k], rHuEPO[k], TSat[k])
\]

In this formula, the index \( k \) denotes a time step, equal to 1 month, and \( f() \) represents a functional relationship. The details of function \( f() \) will be discussed below. Even though this equation is a fundamental component of the simulation and is specified a priori, it is unknown to the \( Q \)-Learning Agent. The function \( f() \) is used in this study exclusively for the purpose of representing the Patient module within the framework presented in Figure 1.

To simulate the Hgb response to rHuEPO, we developed a patient model based on a Takagi-Sugeno (TS) fuzzy system [18]. A TS fuzzy system can be regarded as a collection of local models, whose partial contribution toward the system output is determined by the system input. We use the patient’s resistance to rHuEPO as the input. This quantity is computed as a ratio of the 3-month average rHuEPO dose to the 3-month average level of Hgb. We hypothesized that the Hgb level in individuals with low rHuEPO resistance was governed by different dynamics than those with high rHuEPO resistance. The TS fuzzy system was determined to be an effective tool to represent the imprecise boundary

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Fig. 1. Block diagram of the simulation scenario for reinforcement learning-based anemia management.
between the notions of “low” and “high” rHuEPO resistance. To build the patient model, we used data from 186 patients undergoing hemodialysis at the Division of Nephrology of the Department of Medicine, University of Louisville. Using data records of 12 months containing monthly Hgb levels and rHuEPO doses, we calculated rHuEPO resistance for each individual. We then performed fuzzy c-means clustering [19] and produced fuzzy membership functions categorizing the two types of rHuEPO resistance. These membership functions are shown in Figure 2.

We will subsequently refer to individuals with low rHuEPO resistance as “normal responders” and to individuals with high rHuEPO resistance as “poor responders.” However, a single individual usually exhibits characteristics that combine the features of both response types to a certain degree (µ). For example, someone with rHuEPO resistance of 1.0 is similar to a normal responder to a degree 0.80, and to a poor responder to a degree 0.28.

Having extracted the fuzzy classification of rHuEPO resistance, we created the models (1) for each response group. The data set used to estimate these models contained monthly Hgb, rHuEPO, and TSat values. We used the following linear model:

\[
\text{Hgb}[k + 1] = c_{\text{Hgb}} \text{Hgb}[k] + c_{\text{rHuEPO}} \text{rHuEPO}[k] + c_{\text{TSat}} \text{TSat}[k] + c_{\text{bias}}. \tag{2}
\]

In this model, the coefficients \( c = [c_{\text{Hgb}}, c_{\text{rHuEPO}}, c_{\text{TSat}}, c_{\text{bias}}] \) determine the Hgb response characteristic of that response group. We estimated these coefficients using the weighted least squares method and obtained the following values

\[
c^{\text{high}} = [0.81, 0.03, -0.014, 1.40] \tag{3}
\]

for the high rHuEPO resistance group and

\[
c^{\text{low}} = [0.72, 0.05, -0.006, 3.21] \tag{4}
\]

for the low rHuEPO resistance group.

Using the TS approach [18], the coefficients \( c \) for the individual shown in Figure 2 can now be simply computed in the following way:

\[
c_{\text{Hgb}} = \frac{\mu_{\text{low}} c_{\text{Hgb}}^{\text{low}} + \mu_{\text{high}} c_{\text{Hgb}}^{\text{high}}}{\mu_{\text{low}} + \mu_{\text{high}}} = \frac{0.80 \cdot 0.72 + 0.28 \cdot 0.81}{0.80 + 0.28} = 0.74 \tag{5}
\]

\[
c_{\text{rHuEPO}} = \frac{\mu_{\text{low}} c_{\text{rHuEPO}}^{\text{low}} + \mu_{\text{high}} c_{\text{rHuEPO}}^{\text{high}}}{\mu_{\text{low}} + \mu_{\text{high}}} = \frac{0.80 \cdot 0.81 + 0.28 \cdot 0.72}{0.80 + 0.28} = 0.045 \tag{6}
\]

\[
c_{\text{TSat}} = \frac{\mu_{\text{low}} c_{\text{TSat}}^{\text{low}} + \mu_{\text{high}} c_{\text{TSat}}^{\text{high}}}{\mu_{\text{low}} + \mu_{\text{high}}} = \frac{0.80 \cdot (-0.006) + 0.28 \cdot (-0.014)}{0.80 + 0.28} = -0.008 \tag{7}
\]

\[
c_{\text{bias}} = \frac{\mu_{\text{low}} c_{\text{bias}}^{\text{low}} + \mu_{\text{high}} c_{\text{bias}}^{\text{high}}}{\mu_{\text{low}} + \mu_{\text{high}}} = \frac{0.80 \cdot 3.21 + 0.28 \cdot 1.40}{0.80 + 0.28} = 2.74. \tag{8}
\]

To summarize, the final patient model is a nonlinear weighted combination of the two linear models that define the response for a normal and poor responder.

The Q-learning Agent is capable of learning the dosing strategy regardless of the model structure and its parameters. Therefore, other types of models may be used for this purpose as well [20]–[22]. The above-described model was used in this study because the fuzzy response classification provides a simple and convenient way of representing the characteristics of a patient in terms that are easily recognized in the medical field.

The goal of the agent can be summarized as learning the best dosing policy (Hgb – rHuEPO pairs) using a trial-and-error approach. In much the same way as the physician, the agent recommends a specific rHuEPO dose to be administered and assesses its effect on the Hgb level with respect to the therapeutic goal. The acquired information not only determines the adequacy of the recommended dose but also indicates how it should be modified to improve the response. More specifically, an increase or decrease of the dose amount may be recommended next time the same Hgb level is measured. The agent maintains a dosing policy in the form of a look-up table of current Hgb and recommended rHuEPO dose pairs that will move the Hgb level to the desired range. This look-up table is updated as the agent gains experience. An update to this policy occurs upon observing the change of patient’s Hgb level, following administration of the recommended rHuEPO dose. It can be shown that, under some mild technical assumptions, this algorithm produces an optimal policy [23]; i.e., one that, for each Hgb level, selects the rHuEPO dose that is most beneficial in terms of a long-term treatment outcome. We provide the computational details of this learning scheme next.

![Fig. 2. Fuzzy membership functions for EPO resistance index.](image)
In the proposed simulation scenario, the agent uses a policy defined on finite Hgb and rHuEPO ranges. In the data set of 186 patients used for this study, the Hgb ranged from 7 to 14 g/dL. Laboratory measurements specify Hgb values with accuracy of one decimal place. Hence, the smallest possible increment of the Hgb range would be every 0.1 g/dL. This, however, would greatly increase computation time and is not meaningful from a medical perspective since a step size of 0.1 g/dL is smaller than the measurement error for Hgb. In this work, we represent the Hgb space as a range from 7 to 14 g/dL with a step of 0.5 g/dL. The “Dose Administration” block in Figure 1 is responsible for computing intermediate doses for Hgb levels not represented within the policy. The rHuEPO doses in the data set ranged from 0 to 60,000 units per week. The smallest minimum dose per treatment is 1,000 Units and there are three treatments per week. Therefore, we represented the rHuEPO space as a range from 0 to 60,000 units with a step of 3,000 units.

The experience acquired by the agent is stored within a table computed using the following formula [8]:

\[
Q(Hgb, rHuEPO) = \sum_{k=0}^{\infty} \gamma^k g(Hgb[k], Hgb[k+1]) - Hgb, rHuEPO[0] = rHuEPO
\]

which states that a Q-value for a Hgb/rHuEPO combination is an expected value of the sum of immediate rewards \( g(Hgb[k], Hgb[k+1]) \) for changing the Hgb level from Hgb[k] to Hgb[k+1], discounted by the coefficient \( \gamma \in [0, 1] \). The reward function \( g() \) is the only component of the learning algorithm that links the agent to the control objective. As the treatment goal is to drive the Hgb level to the target interval of 11 to 12 g/dL, we used a \( g() \) function that reinforces all Hgb changes toward that interval and attenuates all Hgb changes away from it. Furthermore, since the observed Hgb is not precisely measured by the analytical technique and varies in time due to other unmeasured factors, we decided to give the strongest reinforcement to any Hgb changes toward the median of the target range. Maintaining the Hgb level close to 11.5 g/dL minimizes the likelihood of Hgb being outside the target range in a real patient. The reward function used in this work is summarized in equation (10), as shown at the bottom of the page.

The Q-value defined by (9) can be viewed as a measure of a long-term benefit from administering a certain dose of rHuEPO at a given Hgb level. In other words, for a set of possible Hgb/rHuEPO combinations, their Q-values simply denote how preferable it is to apply a specific rHuEPO dose at that Hgb level. The higher the Q-value, the more preferable the specific the rHuEPO dose is. We will further denote the most preferred dose by rHuEPO*. Once the table of all possible Q-values (Q-table) is available, rHuEPO* for each Hgb level can be found using a greedy policy search:

\[
rHuEPO^*(Hgb) = \arg \max_{rHuEPO} Q(Hgb, rHuEPO).
\]

Given a Hgb change from Hgb[k] to Hgb[k+1] as a result of administering specific dose rHuEPO[k], together with the incurred reward \( g(Hgb[k], Hgb[k+1]) \), the agent incrementally updates the Q-values [23]:

\[
Q(Hgb[k], rHuEPO[k]) = Q(Hgb[k], rHuEPO[k]) + \alpha(k) g(Hgb[k], Hgb[k+1]) + \gamma \max_{rHuEPO} Q(Hgb[k+1], rHuEPO) - Q(Hgb[k], rHuEPO[k]),
\]

where \( \alpha(k) \) is an exponentially decreasing learning rate. Since the formulation of the reward function (10) does not take into account delayed reinforcement (i.e., only current and not past Hgb changes are being taken into account), the discount coefficient \( \gamma \) does not influence the learning process.

In the standard formulation, the agent updates only the Q-values for Hgb/rHuEPO pairs that are “encountered” during the dosing process. In critical applications, such as this one, this may lead to long learning times, as we have observed in [13]. For the rHuEPO dosing problem described here, it has been known that the response of Hgb to rHuEPO is monotonic and nondecreasing [24]. We propose an extension to the standard Q-learning algorithm that updates the Q-values not only for the current Hgb/rHuEPO combination but also for those combinations that are deemed not preferable, based on the experience acquired by the agent and the assumption of monotonicity. As a result, those rHuEPO doses are less likely to be administered at a further stage, which in turn increases the learning speed. The multiple Q-value updates are performed according to the following heuristic rules:

- If Hgb[k] < 11.5 and Hgb[k+1] ≤ Hgb[k], or Hgb[k] = 11.5 and Hgb[k+1] < Hgb[k] then update \( Q(Hgb, rHuEPO) \) for all Hgb ≤ Hgb[k] and rHuEPO ≤ rHuEPO[k]. In other words, if the current Hgb level is below 11.5 g/dL and the current rHuEPO does not increase or causes a decrease of the Hgb level, or the current Hgb level is 11.5 g/dL and the current rHuEPO causes a decrease of the Hgb level, all doses below and including the current one are inadequate for the current Hgb level and below.

- If Hgb[k] > 11.5 and Hgb[k+1] ≥ Hgb[k], or Hgb[k] = 11.5 and Hgb[k+1] > Hgb[k] then update \( Q(Hgb, rHuEPO) \) for all Hgb ≥ Hgb[k] and rHuEPO ≥ rHuEPO[k]. In other words, if the current Hgb level is above 11.5 g/dL and the current rHuEPO does not decrease or causes an increase of the Hgb level, or the current Hgb level is 11.5 g/dL and the current rHuEPO causes an increase of the Hgb level, all doses above and including the current one are inadequate for the current Hgb level and above.

- Otherwise perform a standard Q-update.

\[
g(Hgb[k], Hgb[k+1]) = \begin{cases} -1, & 11.5 \geq Hgb[k] > Hgb[k+1] \quad \lor \quad Hgb[k+1] > Hgb[k] \geq 11.5 \\ 0.5, & 11.5 > Hgb[k+1] > Hgb[k] \quad \lor \quad Hgb[k] > Hgb[k+1] > 11.5 \\ 1, & Hgb[k+1] = 11.5 \\ 0, & \text{otherwise.} \end{cases}
\]
The proposed extension to the standard $Q$-learning algorithm performs multiple, region-based updates and can be viewed as a form of state abstraction, a general methodology that improves the learning speed. The earliest work on using region-based updates in reinforcement learning was by Yee et al. [25]. In this work, the definition of a region was based on a hierarchical organization of concepts. Dietterich et al. [26] used state abstraction as a component of their algorithms for planning in deterministic and stochastic domains. These methods assumed perfect knowledge about the environment and adaptively created regions to be evaluated during learning. Experiments verified that the region-based updates accelerate learning.

As the $Q$-learning Agent operates on a policy defined on finite Hgb levels, an interface is required to compute intermediate rHuEPO doses; i.e., doses corresponding to Hgb values not represented in the policy. This interface is represented by the Dose Administration block in Figure 1. If we denote a measured Hgb level in the patient by $Hgb_p$, then the corresponding intermediate dose, $rHuEPO_p$, is calculated by Dose Administration simply by performing linear interpolation

$$rHuEPO_p = rHuEPO_l + \frac{Hgb_u - Hgb_p}{Hgb_u - Hgb_l} \times (rHuEPO_u - rHuEPO_l), \quad (13)$$

where the subscripts $l$ and $u$ denote the lower and upper nearest Hgb levels in the policy and their corresponding rHuEPO doses. For example, if $Hgb_p$ is measured as 10.2 g/dL, then $Hgb_l$ is 10.0 g/dL and $Hgb_u$ is 10.5 g/dL. Let us assume that, for a given policy, $rHuEPO_l$ is 21,000 units and $rHuEPO_u$ is 12,000 units. The calculated $rHuEPO_p$ value will then equal 15,600 units, which, after rounding down to multiples of 3,000 units, will give the recommended $rHuEPO$ dose of 15,000 units.

### Preparation of the Data

We evaluated the proposed method using an experimental setup similar to the ones used in [13], [14], and [15]. We first created an artificial population of 100 normal responders and 100 poor responders. For each artificial patient, a set of four initial Hgb values was generated based on the statistics from the above-mentioned patient data from 186 individuals. Since our aim was to test incident patients (i.e., ones that had not received rHuEPO previously), we had to impose their rHuEPO resistance a priori. For normal responders, we randomly generated their degrees of membership in the low rHuEPO resistance group from the range 0.6 to 0.9. Conversely, their degree of membership in the high rHuEPO resistance group was randomly drawn from the range 0.1 to 0.4. Similar procedures were then performed for poor responders. For each patient, the treatment was simulated over a period of 24 months. Before each treatment simulation, we initialized the $Q$-table such that the first policy would represent a so called “best-guess” dosing strategy. This “best guess” strategy is based on a heuristic that low Hgb levels require large rHuEPO doses and vice versa. Following the explanation presented in the Understanding the Data section, we set the discount coefficient $\gamma$ to 0. We set the initial value $\alpha_0$ of the learning rate $\alpha(k)$ to 0.33 and decreased it by $1/k$ in each step. The mean value of TSat, $m_{\text{TSat}}$, for each patient was randomly drawn from the interval 10 to 50% and the standard deviation of TSat, $\sigma_{\text{TSat}}$, was set to 10%. These values were decided upon based on the analysis of our 186 real patients. Furthermore, the TSat variation during the simulated treatment was bounded between 10 – 50%.

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**Fig. 3.** Example of a simulated anemia treatment for a normal responder as performed by standard $Q$-learning: (a) plot of Hgb level; (b) plot of administered rHuEPO.
In the first set of simulations, we applied basic $Q$-learning, i.e., one without multiple $Q$-updates. Subsequently, we repeated the simulations using the proposed extended $Q$-learning algorithm that includes multiple $Q$-updates using the same experimental conditions. We completed the evaluation process by simulating the anemia treatment with a numerical implementation of the AMP currently used at the Division of Nephrology to administer rHuEPO.

To allow for a comparative analysis between the tested methods, we used the following criteria:

- mean Hgb level—to assess the ability to drive the Hgb level to the target range
- standard deviation of Hgb—to determine how well a constant Hgb level is maintained
- number of times Hgb is out of target range—to determine how well the Hgb level is maintained within the target range; i.e., the clinical rate of success
- total rHuEPO used—to determine the cost-effectiveness.

### Data Mining

Figures 3 and 4 show examples of a simulated anemia treatment performed by the standard $Q$-learning for a representative normal responder and poor responder, respectively. These figures demonstrate that the standard $Q$-learning exhibits a tendency to maintain the Hgb level close to the upper bound of the target range in normal responders and close to the lower bound of the target range in poor responders. Figures 5 and 6 show examples of a simulated anemia treatment performed by the extended $Q$-learning method with multiple $Q$-updates for a representative normal responder and a poor responder, respectively. These figures show that the
addition of multiple updates allows for much better control of Hgb level. For both, normal and poor responders, the Hgb level is now much closer to the median of the target range. Hence, one would expect this method to be more effective than the classical $Q$-learning in a real clinical environment. Finally, Figures 7 and 8 show examples of a simulated anemia treatment performed by the numerically implemented AMP. The most striking phenomenon that can be observed in these figures is the Hgb level fluctuation within the target range. This fluctuation occurs for both types of responders. This observation in the simulated environment is consistent with actual data from the clinical environment.

Tables 1 and 2 provide a quantitative comparison between the three simulated methods. The results are reported as means and 95% confidence intervals. Comparing the mean Hgb levels of normal responders between the three methods, we observe that $Q$-learning has a tendency to overcontrol the Hgb level, whereas $Q$-learning with multiple updates and the AMP drive the Hgb level to the target range. Comparing the standard deviations of the Hgb levels for normal responders among the three methods, one can observe that both $Q$-learning methods are more stable than the AMP. Due to the inability of $Q$-learning to maintain the Hgb level within the target range, the third criterion (number of times Hgb is out of target range) has a much larger value for this method compared to the other two. The amounts of administered rHuEPO are not significantly different between the three methods.

Comparing the mean Hgb levels of poor responders among the three methods, we can observe that all three methods are capable of driving the Hgb level to the target range. Comparison of the standard deviations of Hgb levels reveals that, similarly to the case of normal responders, $Q$-learning methods provide more stable Hgb control than the AMP. In terms of the number of times the Hgb level was out of target range, $Q$-learning with multiple updates outperformed the other two competitors. The amounts of administered rHuEPO are again not significantly different among the three methods.
AMP, that has been developed over several years, Our data demonstrate the usefulness of the $Q$-learning methods as applied to drug dosing, where $Q$-learning with multiple updates preformed well based on the metrics that we used to judge between the compared methods.

We found that $Q$-learning is a useful tool to determine appropriate drug dosing schemes used to attain a desired drug concentration or response. In the case that we use to demonstrate these techniques, we are interested in the amount of Hgb in the blood. In general, as more EPO is given to a patient, the amount of Hgb in the blood will rise. However, there is a delay between the administration of the EPO and the change in Hgb level, and the process is further complicated by other factors, like the amount of iron available to make new Hgb. Therefore, the relationship is nonlinear in nature, it changes in time, and we cannot capture all of the variables that impact the Hgb variability. We have used the standard $Q$-learning in a previous application of dosing EPO and noticed several shortcomings that we attempted to address through the use of $Q$-learning with multiple updates. We had found previously that in this specific time-critical application, the standard $Q$-learning is too sensitive to the initial policy. Presented simulation results show that the standard $Q$-learning with multiple updates is not affected by this problem. More specifically, in our previous work, the standard $Q$-learning experienced trouble driving the Hgb level in poor responders into the target range. We were able to overcome this problem in our present work using a different, more aggressive initial policy and observing that, this time, the standard $Q$-learning struggled to drive the Hgb level down toward the target range in normal responders. From a clinical point of view, this is not as troublesome as patients with Hgb below the target range. Nevertheless, we observed that the $Q$-learning with multiple updates, being less sensitive to the initial policy, achieved adequate Hgb response in both normal and poor responders.

Looking at the results of the simulations from a clinical perspective, all three methods are fairly similar in achieving an average Hgb in the two subpopulations (poor and normal responders). The exception to this is that the standard $Q$-learning for normal responders results in an average Hgb of about 12.2 g/dL.

| Table 1. Comparison of anemia treatment simulation results for normal responders. |
|---------------------------------|---------------------------------|---------------------------------|
| Method                          | Standard $Q$-Learning            | $Q$-Learning with Multiple Updates | Anemia Management Protocol |
| Mean Hgb (g/dL)                 | 12.21 (11.77, 12.64)             | 11.77 (11.51, 12.02)             | 11.75 (11.47, 12.02)       |
| Std Dev Hgb (g/dL)              | 0.16 (0.06, 0.26)                | 0.25 (0.09, 0.40)                | 0.50 (0.30, 0.70)          |
| Number of Times Hgb Out of Target Range | 15.4 (2.8, 28.0) | 2.4 (0.0, 8.2) | 2.9 (0.0, 6.6) |
| Total rHuEPO Used (1,000 Units) | 286.3 (200.2, 372.5)             | 227.8 (122.3, 333.3)             | 223.2 (116.9, 329.6)       |

| Table 2. Comparison of anemia treatment simulation results for poor responders. |
|---------------------------------|---------------------------------|---------------------------------|
| Method                          | Standard $Q$-Learning            | $Q$-Learning with Multiple Updates | Anemia Management Protocol |
| Mean Hgb (g/dL)                 | 11.44 (10.96, 11.91)             | 11.46 (11.18, 11.73)             | 11.56 (11.34, 11.77)       |
| Std Dev Hgb (g/dL)              | 0.26 (0.14, 0.37)                | 0.26 (0.12, 0.39)                | 0.58 (0.28, 0.87)          |
| Number of Times Hgb Out of Target Range | 1.3 (0.0, 7.7) | 0.2 (0.0, 0.3) | 2.9 (0.0, 11.0) |
| Total rHuEPO Used (1,000 Units) | 468.1 (351.2, 585.1)             | 469.7 (334.3, 605.3)             | 474.9 (351.2, 585.1)       |
We found that $Q$-learning is a useful tool to help determine appropriate drug dosing strategies for achieving desired drug response.

which is outside the target range and is unacceptable given that the simulation represents a well-behaved environment without the random noise associated with real clinical data. $Q$-learning with multiple updates performs as well as the benchmark AMP and is slightly better in poor responders. The real difference then lies in the approximately 50% decrease in Hgb variability seen in the $Q$-learning with multiple updates, which is clinically significant. Currently, only about one-third of the patients treated with rHuEPO are within the recommended range of 11–12 g/dL Hgb. Decreasing the variability in mean Hgb will increase this percentage, which is a desirable effect.

The cost of EPO to Medicare and Medicaid in 1998 was about US$800 million per year [27]. We compared the total EPO utilization between the $Q$-learning and the AMP to verify whether the former would impact the amount of EPO used, as we have seen in other simulations using machine learning techniques [28]. This was not the case for either of the $Q$-learning methods. However, our formulation of the treatment goal in this study did not factor in the EPO utilization. This point will be of particular interest in further investigation to determine how the reinforcement learning techniques can be applied to enable not only an adequate but also cost-effective treatment of renal anemia.

Summary and Conclusions

We have proposed an extension to the $Q$-learning algorithm that incorporates the existing clinical expertise into the trial-and-error process of acquiring an appropriate administration strategy of rHuEPO to patients with anemia due to ESRD. The specific modification lies in multiple updates of the $Q$-values for several dose/response combinations during a single learning event. This in turn decreases the risk of administering doses that are inadequate in certain situations and thus increases the speed of the learning process. We have evaluated the proposed method using a simulation test-bed involving an “artificial patient” and compared the outcomes to those obtained by a classical $Q$-learning and a numerical implementation of a clinically used administration protocol for anemia management. The outcomes of the simulated treatments demonstrate that the proposed method is a more effective tool than the traditional $Q$-learning. Furthermore, we have observed that it has a potential to provide even more stable anemia management than the AMP.

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